

## The Crystal Structure of *trans*-Dichloridodiaquoethylene-diaminechromium(III) Chloride, *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl

ROLF STOMBERG and INGRID LARKING

Department of Inorganic Chemistry, Chalmers Institute of Technology and University of Göteborg, Fack, S-402 20 Göteborg 5, Sweden

The structure of one of the three possible isomers of [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl has been determined from visually estimated X-ray data by Patterson and Fourier methods and refined by the least-squares technique to a final *R*-value of 0.117 for 866 observed reflexions.

The crystals are orthorhombic, belonging to space group *Pmc2*<sub>1</sub>, with *a*=8.811 Å, *b*=7.539 Å, and *c*=14.256 Å. There are four formula units in the cell. Every chromium atom is octahedrally surrounded by two chlorine atoms in *trans* positions, the two nitrogen atoms of the ethylenediamine molecule, and two water oxygen atoms. The crystals are composed of [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]<sup>+</sup> and Cl<sup>-</sup> ions.

Average bond distances and angles are: Cr—Cl 2.32 Å, Cr—N 2.08 Å, Cr—O 2.05 Å, Cl—Cr—Cl 179.1°, N—Cr—N 83.1° and O—Cr—O 96.7°.

House and Garner<sup>1</sup> have used diperidoamines of chromium(IV) in the synthesis of amine complexes of chromium(III). In particular, they have devised a simpler and more efficient method to synthesize Weinmann's blue, [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl.<sup>2,3</sup> In connection with this work the question has arisen which of the three theoretically possible geometric configurations is adopted by the [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]<sup>+</sup> ion.

The kinetics of aquation of the [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]<sup>+</sup> ion in acid solution has been investigated by these authors<sup>4</sup> in the hope that the kinetic data and identification of aquation products might have been of help in characterizing the geometric configuration. Since the "wet" chemical methods have failed to give a conclusive answer, one of the present authors (R. S.) has been asked by Dr. House to perform the crystal structure analysis of Weinmann's blue.

Table 1. Observed lines in the powder photograph of *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>4</sub>en]Cl.  
 $\lambda(\text{CuK}\alpha_1) = 1.54051 \text{ \AA}$ .

| <i>h k l</i> | $10^5 \times \sin^2\theta_{\text{obs}}$ | $10^5 \times \sin^2\theta_{\text{calc}}$ | $I_{\text{obs}}$ | $d_{\text{obs}}$ |
|--------------|---|--|------------------|------------------|
| 0 0 2        | 1176                                    | 1168                                     | w                | 7.103            |
| 0 1 1        | 1341                                    | 1336                                     | st               | 6.651            |
| 1 1 0        | 1810                                    | 1808                                     | w                | 5.725            |
| 1 0 2        | 1936                                    | 1932                                     | vst              | 5.536            |
| 1 1 1        | 2107                                    | 2100                                     | vst              | 5.307            |
| 0 1 2        | 2216                                    | 2212                                     | m                | 5.174            |
| 1 1 2        | 2974                                    | 2976                                     | vw               | 4.466            |
| 2 0 0        | 3062                                    | 3057                                     | w                | 4.402            |
| 0 1 3        | 3673                                    | 3671                                     | vst              | 4.019            |
| 2 1 0        | 4096                                    | 4100                                     | vvw              | 3.806            |
| 2 0 2        | 4224                                    | 4224                                     | m                | 3.748            |
| 0 2 1        | 4464                                    | 4467                                     | vst              | 3.636            |
| 0 0 4        | 4676                                    | 4671                                     | st               | 3.562            |
| 1 0 4        | 5446                                    | 5435                                     | vvw              | 3.301            |
| 0 1 4        | 5716                                    | 5715                                     | w                | 3.222            |
| 1 1 4        | 6480                                    | 6479                                     | vw               | 3.026            |
| 2 1 3        | 6728                                    | 6728                                     | w                | 2.970            |
| 0 2 3        | 6794                                    | 6803                                     | w                | 2.955            |
| 2 2 1        | 7527                                    | 7524                                     | w                | 2.808            |
| 1 2 3        | 7570                                    | 7567                                     | w                | 2.800            |
| 2 0 4        | 7726                                    | 7728                                     | w                | 2.771            |
| 3 1 0        | 7945                                    | 7921                                     | vvw              | 2.733            |
| 3 0 2        | 8047                                    | 8045                                     | w                | 2.715            |
| 3 1 1        | 8214                                    | 8213                                     | w                | 2.688            |
| 0 1 5        | 8342                                    | 8342                                     | vvw              | 2.667            |
| 2 1 4        | 8776                                    | 8771                                     | m                | 2.600            |
| 1 1 5        | 9116                                    | 9107                                     | vw               | 2.551            |
| 2 2 3        | 9864                                    | 9859                                     | vw               | 2.452            |
| 0 3 2        | 10550                                   | 10562                                    | m                | 2.370            |
| 0 2 5        | 11467                                   | 11474                                    | m                | 2.274            |
| 0 1 6        | 11579                                   | 11554                                    | w                | 2.266            |
| 4 0 0        | 12227                                   | 12226                                    | m                | 2.203            |
| 3 1 4        | 12599                                   | 12592                                    | vvw              | 2.171            |
| 4 1 1        | 13570                                   | 13562                                    | vw               | 2.092            |
| 3 2 3        | 13660                                   | 13680                                    | vvw              | 2.082            |
| 0 3 4        | 14075                                   | 14065                                    | vvw              | 2.054            |
| 4 1 2        | 14443                                   | 14438                                    | vvw              | 2.027            |
| 2 2 5        | 14553                                   | 14530                                    | vvw              | 2.021            |
| 0 2 6        | 14686                                   | 14685                                    | vvw              | 2.010            |
| 1 3 4        | 14841                                   | 14829                                    | vvw              | 2.000            |
| 3 1 5        | 15244                                   | 15220                                    | vvw              | 1.9728           |
| 0 1 7        | 15347                                   | 15349                                    | m                | 1.9662           |
| 4 1 3        | 15911                                   | 15897                                    | m                | 1.9310           |
| 4 2 1        | 16711                                   | 16693                                    | m                | 1.8842           |
| 4 0 4        | 16913                                   | 16897                                    | vw               | 1.8729           |
| 1 2 7        | 19233                                   | 19245                                    | vvw              | 1.7563           |
| 1 0 8        | 19471                                   | 19449                                    | vvw              | 1.7456           |
| 0 1 8        | 19734                                   | 19728                                    | vw               | 1.7339           |
| 1 3 6        | 20654                                   | 20668                                    | vvw              | 1.6948           |
| 0 4 4        | 21388                                   | 21372                                    | vvw              | 1.6655           |
| 4 0 6        | 22743                                   | 22736                                    | vw               | 1.6151           |
| 4 2 5        | 23700                                   | 23700                                    | vvw              | 1.5822           |
| 4 1 6        | 23780                                   | 23780                                    | vvw              | 1.5795           |
| 3 2 7        | 25380                                   | 25358                                    | vvw              | 1.5289           |
| 4 3 4        | 26306                                   | 26291                                    | vvw              | 1.5018           |
| 4 1 7        | 27561                                   | 27575                                    | vw               | 1.4672           |
| 6 0 2        | 28670                                   | 28677                                    | vvw              | 1.4385           |
| 0 0 10       | 29198                                   | 29194                                    | vw               | 1.4255           |
| 4 1 8        | 31943                                   | 31954                                    | vvw              | 1.3628           |

## EXPERIMENTAL

*Preparation and analysis of the crystals.* Crystals of Weinmann's blue, suitable for X-ray diffraction experiments, were produced by the method proposed by House and Garner.<sup>1</sup> Our crystals showed exactly the same X-ray powder pattern as those kindly analyzed and sent to us by Dr. House.

*X-Ray methods.* Accurate cell dimensions were obtained from X-ray powder photographs taken in a Guinier focusing camera with  $\text{CuK}\alpha$  radiation, using  $\text{KCl}$  ( $a=6.2929 \text{ \AA}$  at  $20^\circ\text{C}$ )<sup>5</sup> as an internal standard.

For the single crystal work multiple film (5 films) equi-inclination Weissenberg photographs were taken of crystals of approximate dimensions  $0.1 \times 0.1 \times 0.2 \text{ mm}$  with rotation about [100] (layer lines 0–8) and [001] (layer line 0), using  $\text{CuK}\alpha$  radiation. Three crystals were used.

The relative intensities of the reflexions were estimated visually by comparison with a standard scale (obtained by the rotating sector method) and were corrected using Lorentz' and polarization factors. Absorption and extinction effects were not considered. The  $|F_o|$ -values were brought to an absolute scale by comparison with the finally calculated structure factors.

*Computing methods.* The computational work, including least-squares refinement of the cell dimensions, Lorentz' and polarization corrections, Fourier summations, structure factor least-squares refinements and calculation of interatomic distances and angles, was performed on the electronic computer SAAB D21 using a set of crystallographic programmes written by Abrahamsson, Aleby, Larsson, Lindqvist and Wengelin.<sup>6–11</sup>

The atomic scattering factors used in the calculation of the structure factors were taken from Volume III of the *International Tables for X-ray Crystallography*, 1962.

## UNIT CELL AND SPACE GROUP

The unit cell parameters were obtained from the measured  $\sin^2\theta$  values by a least-squares procedure using 59 observed lines.  $[\text{CrCl}_2(\text{H}_2\text{O})_2\text{en}]\text{Cl}$  was then found to be orthorhombic with

$a=8.811 \pm 0.003 \text{ \AA}$ ,  $b=7.539 \pm 0.006 \text{ \AA}$ ,  $c=14.256 \pm 0.006 \text{ \AA}$ ,  $V=947.0 \text{ \AA}^3$ . (The errors given are  $3\sigma$ ).

Calculated and observed  $\sin^2\theta$  values are given in Table 1.

The systematically absent reflexions were

$h0l$  with  $l=2n+1$

and  $h00$  with  $h=2n+1$

The first condition is characteristic of the space groups  $Pmc2_1$  (No. 26),  $P2cm$  (No. 28), and  $Pmcm$  (No. 51). The second condition does not apply to anyone of the ordinary space groups. It is taken to be "accidental" but it has, of course, a significant structural meaning (see below).

The density of the crystals, determined by weighing a sample in air and benzene, is  $1.71 \text{ g/cm}^3$ . The density calculated for a unit cell containing four formula units is  $1.73 \text{ g/cm}^3$ .

## STRUCTURE DETERMINATION

*Atomic positions.* The Patterson function  $P(uvw)$  showed the following large maxima:

| <i>u</i>      | <i>v</i>      | <i>w</i>      | peak height<br>(arbitrary<br>units) | <i>u</i>      | <i>v</i>      | <i>w</i>      | peak height<br>(arbitrary<br>units) |
|---------------|---------------|---------------|-------------------------------------|---------------|---------------|---------------|-------------------------------------|
| 0             | 0             | 0             | 3826                                | $\frac{1}{2}$ | 0.20          | 0.30          | 855                                 |
| 0.26          | 0             | 0             | 1455                                | 0.26          | 0.29          | $\frac{1}{2}$ | 628                                 |
| 0             | 0.27          | $\frac{1}{2}$ | 1394                                | 0.24          | $\frac{1}{2}$ | 0.20          | 615                                 |
| $\frac{1}{2}$ | 0             | 0             | 1333                                | $\frac{1}{2}$ | 0.24          | $\frac{1}{2}$ | 595                                 |
| $\frac{1}{2}$ | $\frac{1}{2}$ | 0.20          | 1052                                | 0.24          | 0.21          | 0.30          | 404                                 |

The above-mentioned fact that  $h00$  reflexions are observed only for  $h=2n$  means that if the  $x$  value of the position of one atom is  $x_1$ , there will be an atom of the same kind (but not necessarily symmetry-related) at, or very near,  $x_1 + \frac{1}{2}$ . This is consistent with the fact that  $P(uvw)$  has many large maxima at  $u=0$  and  $\frac{1}{2}$ . Since all the remaining heavy peaks of  $P(uvw)$  have  $u \approx \frac{1}{2}$  the space group has at least approximate mirror planes perpendicular to the  $a$  axis at  $x=0$  and  $\frac{1}{2}$ . This makes it probable that the space group is either  $Pmc2_1$  or  $Pmcm$  with the chromium and chlorine atoms in planes at  $x=0$ ,  $\frac{1}{2}$ ,  $\frac{1}{2}$ , and  $\frac{3}{4}$ . From this and space considerations one can conclude that the chromium atoms are situated in the mirror planes, the four chromium atoms in the cell thus occupying two two-fold positions. Comparison between calculated and observed interatomic vectors, with due account taken of possible interatomic distances, indicates that the only possible space group is  $Pmc2_1$  with the following chromium positions:

$Cr_1$  in  $Pmc2_1$ :  $2b$  with  $x = \frac{1}{2}$ ,  $y = 0.13$ ,  $z = 0.30$   
 $Cr_2$  » »  $2a$  »  $x = 0$ ,  $y = 0.33$ ,  $z = 0$

The structure was then solved in the usual, rather straightforward, manner. It was quite obvious that the highest Patterson peak (at 0.26, 0, 0) with the length 2.3 Å, which is a normal Cr—Cl bond length, could be interpreted as overlapping Cr—Cl vectors. The coordinated chlorine atoms would consequently occupy two four-fold positions with the same  $y$  and  $z$  coordinates as the chromium atoms and the  $x$  values 0.24 and 0.26. Probable coordinates for the two chlorine atoms of the asymmetric unit would thus be:

$Cl_1$  in  $Pmc2_1$ :  $4c$  with  $x = 0.24$ ,  $y = 0.13$ ,  $z = 0.30$   
 $Cl_2$  » »  $4c$  »  $x = 0.26$ ,  $y = 0.33$ ,  $z = 0$

A Fourier summation of the observed structure factors was then undertaken with the signs of the Fourier coefficients being determined by the contribution from the atoms  $Cr_1$ ,  $Cr_2$ ,  $Cl_1$ , and  $Cl_2$ . This showed large peaks at all the above positions with relative magnitudes expected for the chromium and chlorine atoms. There were also minor peaks in the mirror planes about the chromium positions. These were taken to be the oxygen and nitrogen sites. Possible positions of the remaining chlorine atoms were found both at  $x=0$  and  $\frac{1}{2}$  and  $x=\frac{1}{4}$  and  $\frac{3}{4}$ . Calculation of  $F(h00)$  values and comparison with observed structure factors made it obvious that the chloride ions occupy the position  $Cl_3$  in  $Pmc2_1$ :  $4c$  with  $x=0.25$ ,  $y=0.61$ ,  $z=0.24$ .

As the nitrogen atoms form tetrahedral bonds in the ethylenediamine molecule and as they lie in the mirror plane containing the chromium and

oxygen atoms, the carbon atoms must be out of this plane. There are two possible solutions to this problem. One is that the correct space group is the monoclinic one *Pc*. The other is to assume that the four carbon atoms of the unit cell statistically occupy two four-fold positions of *Pmc2*<sub>1</sub>. The contribution from the carbon atoms to the structure factors is so small that it is impos-

Table 2a. Atomic coordinates (expressed in fractions of the cell edges) and isotropic thermal parameters with their standard deviations for *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl.

The temperature factor =  $\exp[-B(\sin^2\theta)/\lambda^2]$ . Space group *Pmc2*<sub>1</sub>. 4 molecules in the unit cell. All atoms occupy the twofold positions 2a and 2b except Cl and C which occupy the position 4c.

| Atom            | x             | y      | z      | B<br>Å <sup>2</sup> | $\sigma(x)$<br>$\times 10^4$ | $\sigma(y)$<br>$\times 10^4$ | $\sigma(z)$<br>$\times 10^4$ | $\sigma(B)$<br>Å <sup>2</sup> |
|-----------------|---------------|--------|--------|---------------------|------------------------------|------------------------------|------------------------------|-------------------------------|
| Cr <sub>1</sub> | $\frac{1}{2}$ | 0.1311 | 0.3172 |                     | 6                            | 4                            |                              |                               |
| Cr <sub>2</sub> | 0             | 0.3315 | 0.0134 |                     | 6                            | 4                            |                              |                               |
| Cl <sub>1</sub> | 0.2372        | 0.1296 | 0.3167 |                     | 6                            | 7                            | 4                            |                               |
| Cl <sub>2</sub> | 0.2637        | 0.6707 | 0.5145 |                     | 5                            | 7                            | 4                            |                               |
| Cl <sub>3</sub> | 0.2547        | 0.6094 | 0.2395 |                     | 7                            | 7                            | 6                            |                               |
| O <sub>1</sub>  | $\frac{1}{2}$ | 0.2895 | 0.2027 | 4.20                | 27                           | 16                           | 0.39                         |                               |
| O <sub>2</sub>  | $\frac{1}{2}$ | 0.8945 | 0.2483 | 4.31                | 25                           | 16                           | 0.39                         |                               |
| O <sub>3</sub>  | 0             | 0.5540 | 0.1009 | 4.23                | 27                           | 15                           | 0.40                         |                               |
| O <sub>4</sub>  | 0             | 0.5318 | 0.3910 | 3.67                | 25                           | 14                           | 0.36                         |                               |
| N <sub>1</sub>  | $\frac{1}{2}$ | 0.0001 | 0.4457 | 3.45                | 32                           | 17                           | 0.39                         |                               |
| N <sub>2</sub>  | $\frac{1}{2}$ | 0.3578 | 0.4051 | 3.93                | 30                           | 18                           | 0.46                         |                               |
| N <sub>3</sub>  | 0             | 0.1786 | 0.1346 | 4.05                | 32                           | 19                           | 0.46                         |                               |
| N <sub>4</sub>  | 0             | 0.9085 | 0.4466 | 3.56                | 29                           | 17                           | 0.42                         |                               |
| C <sub>1</sub>  | 0.5415        | 0.8867 | 0.0199 | 4.99                | 47                           | 47                           | 34                           | 0.96                          |
| C <sub>2</sub>  | 0.5406        | 0.2984 | 0.5098 | 6.59                | 55                           | 63                           | 45                           | 1.18                          |
| C <sub>3</sub>  | 0.0368        | 0.9894 | 0.1213 | 7.84                | 70                           | 84                           | 43                           | 1.47                          |
| C <sub>4</sub>  | 0.0312        | 0.9419 | 0.0112 | 4.39                | 43                           | 43                           | 30                           | 0.73                          |

Table 2b. Anisotropic temperature parameters  $U_{ij}$  (with their standard deviations in parentheses). The expression used is

$$\exp -2\pi^2(h^2a^{*2}U_{11}+k^2b^{*2}U_{22}+l^2c^{*2}U_{33}+2klb*c*U_{23}+2lhc*a*U_{31}+2hka*b*U_{12}).$$

| Atom            | $U_{11}$         | $U_{22}$         | $U_{33}$         | $U_{23}$          | $U_{31}$          | $U_{12}$          |
|-----------------|------------------|------------------|------------------|-------------------|-------------------|-------------------|
| Cr <sub>1</sub> | 0.055<br>(0.003) | 0.043<br>(0.002) | 0.034<br>(0.002) | 0.005<br>(0.002)  | 0                 | 0                 |
| Cr <sub>2</sub> | 0.045<br>(0.002) | 0.047<br>(0.002) | 0.037<br>(0.002) | -0.006<br>(0.002) | 0                 | 0                 |
| Cl <sub>1</sub> | 0.043<br>(0.002) | 0.059<br>(0.003) | 0.057<br>(0.003) | 0.014<br>(0.003)  | -0.005<br>(0.003) | -0.005<br>(0.002) |
| Cl <sub>2</sub> | 0.038<br>(0.003) | 0.067<br>(0.003) | 0.056<br>(0.003) | 0.013<br>(0.003)  | 0.008<br>(0.003)  | -0.001<br>(0.002) |
| Cl <sub>3</sub> | 0.052<br>(0.003) | 0.063<br>(0.003) | 0.062<br>(0.003) | -0.004<br>(0.003) | 0.000<br>(0.003)  | -0.005<br>(0.003) |

Table 3. Observed and calculated structure factors for *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl. The columns are successively *h*, *k*, *l*, 100|*F*<sub>o</sub>|, 100|*F*<sub>c</sub>|, and phase angle  $\alpha$  (expressed in fractions of one revolution).

|   |    |       |          |        |        |   |   |      |       |        |        |        |    |      |      |        |        |        |
|---|----|-------|----------|--------|--------|---|---|------|-------|--------|--------|--------|----|------|------|--------|--------|--------|
| 0 | 2  | 5563  | 4523     | 0.7476 | 0      | 8 | 3 | 684  | 721   | 1.6417 | 1      | 7      | 1  | 610  | 467  | 0.3724 |        |        |
| 0 | 4  | 15335 | 14631    | 0.6957 | 0      | 8 | 4 | 815  | 706   | 0.3136 | 1      | 7      | 2  | 610  | 649  | 0.2578 |        |        |
| 0 | 6  | 5930  | 6631     | 0.0157 | 0      | 8 | 5 | 1537 | 1368  | 0.8975 | 1      | 7      | 3  | 784  | 802  | 0.2714 |        |        |
| 0 | 6  | 2803  | 2603     | 0.7659 | 0      | 8 | 6 | 966  | 991   | 0.7371 | 1      | 7      | 4  | 984  | 871  | 0.5816 |        |        |
| 0 | 10 | 5259  | 5248     | 0.0158 | 0      | 8 | 7 | 815  | 814   | 0.6770 | 1      | 7      | 5  | 314  | 79   | 0.0995 |        |        |
| 0 | 12 | 3083  | 3675     | 0.9448 | 0      | 8 | 9 | 127  | 149   | 0.0152 | 1      | 7      | 6  | 1008 | 1106 | 0.1111 |        |        |
| 0 | 14 | 4475  | 4188     | 0.3303 | 0      | 8 | 9 | 1121 | 1063  | 1.0010 | 1      | 7      | 7  | 1299 | 1265 | 0.3072 |        |        |
| 0 | 16 | 3500  | 2848     | 0.1977 | 0      | 8 | 9 | 2    | 830   | 964    | 0.6868 | 1      | 7  | 8    | 535  | 534    | 0.0470 |        |
| 0 | 1  | 352   | 259      | 0.5952 | 0      | 8 | 9 | 2    | 812   | 1052   | 0.9458 | 1      | 7  | 9    | 499  | 592    | 0.2682 |        |
| 0 | 1  | 7357  | 6758     | 0.1746 | 0      | 8 | 9 | 761  | 761   | 0.0159 | 1      | 7      | 10 | 524  | 664  | 0.4875 |        |        |
| 0 | 1  | 7357  | 6798     | 0.4480 | 0      | 8 | 9 | 4    | 655   | 867    | 0.1721 | 1      | 8  | 0    | 1448 | 1533   | 0.1111 |        |
| 0 | 1  | 11048 | 13132    | 0.2921 | 0      | 8 | 9 | 5    | 766   | 816    | 0.8994 | 1      | 8  | 1    | 782  | 734    | 0.7834 |        |
| 0 | 1  | 7197  | 6642     | 0.3772 | 0      | 8 | 9 | 6    | 899   | 973    | 0.9558 | 1      | 8  | 2    | 695  | 746    | 0.6498 |        |
| 0 | 1  | 4919  | 4510     | 0.0215 | 1      | 0 | 0 | 2    | 11027 | 9905   | 0.0952 | 1      | 8  | 3    | 801  | 666    | 0.7039 |        |
| 0 | 1  | 9478  | 9478     | 0.8516 | 1      | 0 | 0 | 2    | 2707  | 2707   | 0.0159 | 1      | 8  | 4    | 618  | 617    | 0.4124 |        |
| 0 | 1  | 11033 | 12023    | 0.0149 | 1      | 0 | 0 | 6    | 283   | 338    | 0.0158 | 1      | 8  | 5    | 575  | 575    | 0.0157 |        |
| 0 | 1  | 8762  | 7277     | 0.5984 | 1      | 0 | 0 | 8    | 4038  | 5130   | 0.0123 | 1      | 9  | 1    | 473  | 528    | 0.0485 |        |
| 0 | 1  | 3399  | 3721     | 0.1732 | 1      | 0 | 0 | 10   | 703   | 805    | 0.8493 | 1      | 9  | 2    | 730  | 531    | 0.5995 |        |
| 0 | 1  | 691   | 1059     | 0.3423 | 1      | 0 | 0 | 12   | 2032  | 2100   | 0.2635 | 1      | 9  | 3    | 543  | 521    | 0.7421 |        |
| 0 | 1  | 5850  | 3581     | 0.3422 | 1      | 0 | 0 | 14   | 1154  | 1388   | 0.0750 | 2      | 0  | 0    | 8329 | 744    | 0.3536 |        |
| 0 | 1  | 1239  | 1922     | 0.0111 | 1      | 0 | 0 | 16   | 497   | 570    | 0.0152 | 2      | 0  | 1    | 654  | 694    | 0.5744 |        |
| 0 | 1  | 2376  | 2497     | 0.4215 | 1      | 0 | 0 | 8    | 6362  | 5194   | 0.5000 | 0      | 6  | 1    | 1455 | 1663   | 0.8150 |        |
| 0 | 1  | 1064  | 1016     | 0.5602 | 1      | 0 | 0 | 1    | 8067  | 7573   | 0.1879 | 0      | 8  | 2    | 1312 | 1404   | 0.3576 |        |
| 0 | 1  | 1111  | 1251     | 0.3218 | 1      | 0 | 0 | 2    | 3092  | 2665   | 0.2227 | 0      | 10 | 10   | 1666 | 1853   | 0.9738 |        |
| 0 | 1  | 623   | 1440     | 0.1403 | 1      | 0 | 0 | 3    | 195   | 1716   | 0.2728 | 0      | 12 | 12   | 1675 | 1559   | 0.3942 |        |
| 0 | 1  | 4778  | 4046     | 0.0156 | 1      | 0 | 0 | 4    | 3742  | 3742   | 0.0156 | 0      | 14 | 14   | 3699 | 3699   | 0.0156 |        |
| 0 | 1  | 952   | 1204     | 0.7292 | 1      | 0 | 0 | 5    | 4030  | 3638   | 0.0181 | 1      | 16 | 16   | 1142 | 1112   | 0.2461 |        |
| 0 | 2  | 846   | 1664     | 0.5090 | 1      | 0 | 0 | 6    | 818   | 953    | 0.4888 | 1      | 0  | 1    | 5715 | 5653   | 1.0000 |        |
| 0 | 2  | 13871 | 15202    | 0.6117 | 1      | 0 | 0 | 7    | 3061  | 2496   | 0.1986 | 1      | 1  | 1    | 3530 | 3376   | 0.5714 |        |
| 0 | 2  | 3712  | 3409     | 0.5803 | 1      | 0 | 0 | 9    | 3819  | 3752   | 0.4847 | 1      | 2  | 2    | 2976 | 2668   | 0.3429 |        |
| 0 | 3  | 9225  | 7745     | 0.1759 | 1      | 0 | 0 | 10   | 1424  | 1228   | 0.6101 | 1      | 3  | 3    | 6559 | 5559   | 0.5652 |        |
| 0 | 4  | 4403  | 4297     | 0.5815 | 1      | 0 | 0 | 11   | 1751  | 1593   | 0.9293 | 1      | 4  | 4    | 7105 | 6775   | 0.9477 |        |
| 0 | 5  | 15541 | 12834    | 0.8115 | 1      | 0 | 0 | 12   | 782   | 767    | 0.0156 | 1      | 5  | 5    | 1238 | 1149   | 0.3167 |        |
| 0 | 6  | 6345  | 5882     | 0.5767 | 1      | 0 | 0 | 14   | 1189  | 1277   | 0.8491 | 1      | 6  | 6    | 1647 | 1659   | 0.5443 |        |
| 0 | 7  | 36654 | 4131     | 0.7855 | 1      | 0 | 0 | 15   | 1153  | 1221   | 0.4466 | 1      | 7  | 7    | 2759 | 2508   | 0.6978 |        |
| 0 | 8  | 18624 | 18624    | 0.5899 | 1      | 0 | 0 | 16   | 672   | 681    | 0.6196 | 1      | 8  | 8    | 2058 | 1970   | 0.4978 |        |
| 0 | 9  | 3699  | 4136     | 0.5792 | 1      | 0 | 0 | 17   | 452   | 455    | 0.0156 | 1      | 9  | 9    | 3319 | 3139   | 0.4117 |        |
| 0 | 10 | 4039  | 2225     | 0.4470 | 1      | 0 | 0 | 2    | 2880  | 2961   | 1.0010 | 2      | 11 | 11   | 1368 | 1299   | 0.6156 |        |
| 0 | 11 | 7124  | 6011     | 0.8177 | 1      | 0 | 0 | 1    | 866   | 743    | 0.7870 | 2      | 12 | 12   | 457  | 617    | 0.9470 |        |
| 0 | 12 | 7295  | 1126     | 0.6716 | 1      | 0 | 0 | 2    | 649   | 1088   | 0.4465 | 2      | 14 | 14   | 697  | 810    | 0.2886 |        |
| 0 | 13 | 1226  | 1252     | 0.2988 | 1      | 0 | 0 | 3    | 6704  | 5973   | 0.7321 | 2      | 16 | 16   | 434  | 616    | 0.9419 |        |
| 0 | 14 | 3684  | 3268     | 0.5882 | 1      | 0 | 0 | 4    | 2311  | 2311   | 0.0156 | 2      | 17 | 17   | 3235 | 3235   | 0.0156 |        |
| 0 | 15 | 1105  | 866      | 0.7727 | 1      | 0 | 0 | 5    | 847   | 488    | 0.3127 | 2      | 18 | 18   | 2313 | 2108   | 1.0100 |        |
| 0 | 16 | 3866  | 3848     | 1.0000 | 1      | 0 | 0 | 6    | 1205  | 1203   | 0.4023 | 2      | 19 | 19   | 7212 | 6900   | 0.0520 |        |
| 0 | 17 | 4259  | 3863     | 0.8403 | 1      | 0 | 0 | 7    | 5395  | 5391   | 0.9311 | 2      | 20 | 20   | 3829 | 3591   | 0.9474 |        |
| 0 | 18 | 18879 | 10300    | 0.3776 | 1      | 0 | 0 | 8    | 654   | 870    | 0.6473 | 2      | 21 | 21   | 6017 | 5088   | 0.4947 |        |
| 0 | 19 | 4039  | 2225     | 0.4470 | 1      | 0 | 0 | 9    | 2680  | 2680   | 0.0156 | 2      | 22 | 22   | 4160 | 4160   | 0.0156 |        |
| 0 | 20 | 1139  | 10224    | 0.5803 | 1      | 0 | 0 | 10   | 1190  | 1151   | 0.7303 | 2      | 23 | 23   | 5604 | 5140   | 0.3555 |        |
| 0 | 21 | 4114  | 4531     | 0.2969 | 1      | 0 | 0 | 11   | 686   | 688    | 0.0166 | 2      | 24 | 24   | 1184 | 1015   | 0.6401 |        |
| 0 | 22 | 5245  | 5317     | 0.1156 | 1      | 0 | 0 | 12   | 1264  | 1440   | 0.8491 | 2      | 25 | 25   | 2298 | 1899   | 0.4872 |        |
| 0 | 23 | 3104  | 2970     | 0.2407 | 1      | 0 | 0 | 13   | 693   | 656    | 0.1717 | 2      | 26 | 26   | 3099 | 2837   | 0.9993 |        |
| 0 | 24 | 4446  | 6459     | 0.2406 | 1      | 0 | 0 | 14   | 1077  | 1087   | 0.6099 | 2      | 27 | 27   | 4211 | 116    | 0.2170 |        |
| 0 | 25 | 4354  | 4783     | 0.3431 | 1      | 0 | 0 | 15   | 1078  | 1078   | 0.1599 | 2      | 28 | 28   | 2907 | 1927   | 0.5997 |        |
| 0 | 26 | 2934  | 2995     | 0.4473 | 1      | 0 | 0 | 16   | 609   | 546    | 0.3240 | 2      | 29 | 29   | 1434 | 1321   | 0.8978 |        |
| 0 | 27 | 1206  | 1267     | 0.2954 | 1      | 0 | 0 | 17   | 492   | 533    | 0.9121 | 2      | 30 | 30   | 459  | 543    | 0.2226 |        |
| 0 | 28 | 1407  | 1649     | 0.4108 | 1      | 0 | 0 | 18   | 3229  | 3423   | 0.6930 | 2      | 31 | 31   | 847  | 1610   | 0.6736 |        |
| 0 | 29 | 4347  | 3888     | 0.7666 | 1      | 0 | 0 | 19   | 654   | 870    | 0.6473 | 2      | 32 | 32   | 430  | 488    | 0.3575 |        |
| 0 | 30 | 1122  | 2222     | 0.2525 | 1      | 0 | 0 | 20   | 654   | 654    | 0.1421 | 2      | 33 | 33   | 678  | 545    | 0.3953 |        |
| 0 | 31 | 4414  | 4141     | 0.0141 | 1      | 0 | 0 | 21   | 567   | 567    | 0.0151 | 2      | 34 | 34   | 1050 | 1493   | 0.3555 |        |
| 0 | 32 | 3002  | 2873     | 0.3934 | 1      | 0 | 0 | 22   | 359   | 3883   | 0.0117 | 2      | 35 | 35   | 350  | 359    | 0.5495 |        |
| 0 | 33 | 13    | 1806     | 1469   | 0.4422 | 1 | 0 | 0    | 23    | 1958   | 2086   | 0.1140 | 2  | 36   | 36   | 1210   | 1130   | 0.3535 |
| 0 | 34 | 2136  | 2190     | 0.8836 | 1      | 0 | 0 | 24   | 1829  | 1940   | 0.2430 | 2      | 37 | 37   | 1121 | 1142   | 0.4876 |        |
| 0 | 35 | 2156  | 1940     | 0.8423 | 1      | 0 | 0 | 25   | 3209  | 3361   | 0.5930 | 2      | 38 | 38   | 558  | 618    | 0.4176 |        |
| 0 | 36 | 1515  | 1955     | 0.5548 | 1      | 0 | 0 | 26   | 3213  | 3083   | 0.2425 | 2      | 39 | 39   | 2448 | 2750   | 1.0000 |        |
| 0 | 37 | 3240  | 3249     | 0.5530 | 1      | 0 | 0 | 27   | 775   | 917    | 0.0150 | 2      | 40 | 40   | 1243 | 1136   | 0.8876 |        |
| 0 | 38 | 1630  | 3730     | 0.9278 | 1      | 0 | 0 | 28   | 751   | 520    | 0.7500 | 2      | 41 | 41   | 1194 | 1225   | 0.5922 |        |
| 0 | 39 | 2661  | 2670     | 0.3925 | 1      | 0 | 0 | 29   | 642   | 707    | 0.2806 | 2      | 42 | 42   | 1541 | 1448   | 0.9978 |        |
| 0 | 40 | 6061  | 6305     | 0.7951 | 1      | 0 | 0 | 30   | 669   | 733    | 0.4791 | 2      | 43 | 43   | 1291 | 1363   | 0.9926 |        |
| 0 | 41 | 3392  | 3073     | 0.0133 | 1      | 0 | 0 | 31   | 703   | 656    | 0.3714 | 2      | 44 | 44   | 1223 | 1240   | 0.3535 |        |
| 0 | 42 | 3945  | 3956     | 0.5598 | 1      | 0 | 0 | 32   | 932   | 806    | 0.0158 | 2      | 45 | 45   | 1171 | 1144   | 0.7814 |        |
| 0 | 43 | 7189  | 4119     | 0.8803 | 1      | 0 | 0 | 33   | 882   | 846    | 0.3059 | 2      | 46 | 46   | 1322 | 1397   | 0.6469 |        |
| 0 | 44 | 2362  | 2219     | 0.8669 | 1      | 0 | 0 | 34   | 1235  | 1512   | 0.7948 | 2      | 47 | 47   | 1477 | 1477   | 0.9445 |        |
| 0 | 45 | 2436  | 2533     | 0.7140 | 1      | 0 | 0 | 35   | 1069  | 1215   | 0.4461 | 2      | 48 | 48   | 1050 | 1163   | 0.3626 |        |
| 0 | 46 | 1141  | 1433     | 0.5834 | 1      | 0 | 0 | 36   | 966   | 1122   | 0.5145 | 2      | 49 | 49   | 322  | 516    | 0.4230 |        |
| 0 | 47 | 1517  | 1326     | 0.1717 | 1      | 0 | 0 | 37   | 1054  | 1384   | 0.6140 | 2      | 50 | 50   | 2351 | 2351   | 0.0100 |        |
| 0 | 48 | 1280  | 1590     | 0.6734 | 1      | 0 | 0 | 38   | 620   | 635    | 0.7567 | 2      | 51 | 51   | 947  | 853    | 0.1000 |        |
| 0 | 49 | 1493  | 1847     | 0.1352 | 1      | 0 | 0 | 39   | 442   | 462    | 0.6485 | 2      | 52 | 52   | 1704 | 1718   | 0.5638 |        |
| 0 | 50 | 1599  | 1838     | 0.2428 | 1      | 0 | 0 | 40   | 899   | 744    | 1.0000 | 2      | 53 | 53   | 636  | 747    | 0.5154 |        |
| 0 | 51 | 1242  | 1349     | 0.7134 | 1      | 0 | 0 | 41   | 1658  | 1662   | 0.5796 | 2      | 54 | 54   | 898  | 1157   | 0.4343 |        |
| 0 | 52 | 1304  | 1145     | 0.8802 | 1      | 0 | 0 | 42   | 293   | 1971   | 0.1512 | 2      | 55 | 55   | 562  | 592    | 0.5920 |        |
| 0 | 53 | 2354  | 3350     | 0.6160 | 1      | 0 | 0 | 43   | 675   | 614    | 0.8752 | 2      | 56 | 56   | 1720 | 1892   | 0.8733 |        |
| 0 | 54 | 1420  | 1345</td |        |        |   |   |      |       |        |        |        |    |      |      |        |        |        |

Table 3. Continued.

|   |   |      |      |        |        |   |    |       |       |        |        |        |    |     |      |        |        |        |        |
|---|---|------|------|--------|--------|---|----|-------|-------|--------|--------|--------|----|-----|------|--------|--------|--------|--------|
| 8 | 1 | 642  | 841  | 0.5227 | 3      | 9 | 3  | 523   | 613   | 0.7480 | 3      | 1      | 1  | 1   | 1535 | 1994   | 0.1976 |        |        |
| 6 | 2 | 492  | 633  | 0.9311 | 4      | 6 | 2  | 2766  | 3009  | 0.7294 | 5      | 1      | 2  | 2   | 730  | 758    | 0.2774 |        |        |
| 5 | 3 | 492  | 519  | 0.7177 | 4      | 6 | 4  | 12894 | 8297  | 0.5921 | 5      | 1      | 3  | 3   | 46   | 51     | 0.1152 |        |        |
| 4 | 4 | 382  | 283  | 0.5226 | 4      | 6 | 6  | 1654  | 1640  | 0.0471 | 5      | 1      | 4  | 4   | 837  | 1579   | 0.1388 |        |        |
| 3 | 5 | 367  | 492  | 0.4797 | 4      | 9 | 8  | 1655  | 1640  | 0.0471 | 5      | 1      | 5  | 5   | 1224 | 729    | 0.3382 |        |        |
| 2 | 6 | 348  | 457  | 0.4110 | 4      | 0 | 10 | 7213  | 6423  | 0.1829 | 5      | 1      | 6  | 6   | 411  | 334    | 0.3700 |        |        |
| 1 | 7 | 656  | 633  | 1.0000 | 4      | 0 | 12 | 2427  | 2324  | 0.9971 | 5      | 1      | 7  | 7   | 1207 | 997    | 0.1437 |        |        |
| 0 | 8 | 977  | 1269 | 0.2123 | 4      | 0 | 14 | 2906  | 3197  | 0.3284 | 5      | 1      | 8  | 9   | 1923 | 1467   | 0.4777 |        |        |
| 1 | 9 | 2232 | 1703 | 0.8653 | 4      | 0 | 16 | 2000  | 2024  | 0.4444 | 5      | 1      | 10 | 10  | 700  | 515    | 0.2222 |        |        |
| 2 | 0 | 4    | 2372 | 1978   | 0.2458 | 4 | 1  | 8     | 589   | 834    | 0.5000 | 5      | 1  | 11  | 521  | 568    | 0.1972 |        |        |
| 3 | 1 | 6648 | 5806 | 0.0429 | 4      | 1 | 1  | 3492  | 4451  | 0.3614 | 5      | 1      | 12 | 622 | 264  | 0.4711 |        |        |        |
| 2 | 0 | 10   | 507  | 0.9283 | 4      | 1 | 2  | 4579  | 4743  | 0.6462 | 5      | 1      | 13 | 15  | 420  | 470    | 0.4559 |        |        |
| 3 | 1 | 3249 | 251  | 0.2198 | 4      | 1 | 3  | 8454  | 8281  | 0.2990 | 5      | 1      | 14 | 16  | 345  | 305    | 0.6548 |        |        |
| 2 | 0 | 12   | 1598 | 0.7013 | 4      | 1 | 4  | 403   | 404   | 0.3555 | 5      | 1      | 15 | 16  | 249  | 245    | 0.3949 |        |        |
| 3 | 1 | 16   | 731  | 683    | 0.4994 | 4 | 1  | 5     | 2515  | 2595   | 0.0800 | 5      | 1  | 16  | 1    | 314    | 195    | 0.4241 |        |
| 2 | 0 | 1    | 5496 | 535    | 0.5000 | 4 | 1  | 6     | 5357  | 528    | 0.8289 | 5      | 1  | 2   | 2    | 381    | 347    | 0.4770 |        |
| 3 | 1 | 1    | 6673 | 7564   | 0.1772 | 4 | 1  | 7     | 6559  | 7104   | 0.4117 | 5      | 1  | 2   | 3    | 1893   | 1850   | 0.7012 |        |
| 2 | 1 | 2152 | 2394 | 0.2336 | 4      | 1 | 8  | 5178  | 5235  | 0.5289 | 5      | 1      | 3  | 4   | 1089 | 1615   | 0.5134 |        |        |
| 3 | 1 | 3    | 1747 | 1747   | 0.3737 | 4 | 1  | 9     | 2616  | 2712   | 0.3137 | 5      | 1  | 5   | 5    | 354    | 250    | 0.2202 |        |
| 2 | 0 | 4    | 4583 | 3883   | 0.6433 | 4 | 1  | 10    | 515   | 589    | 0.3993 | 5      | 1  | 6   | 6    | 696    | 738    | 0.3949 |        |
| 3 | 1 | 5    | 5126 | 4445   | 0.3376 | 4 | 1  | 11    | 3607  | 2683   | 0.5995 | 5      | 1  | 7   | 7    | 2574   | 1868   | 0.9955 |        |
| 2 | 0 | 6    | 1223 | 1527   | 0.4926 | 4 | 1  | 12    | 1753  | 1504   | 0.6980 | 5      | 1  | 8   | 8    | 698    | 305    | 0.5978 |        |
| 3 | 1 | 7    | 1000 | 2446   | 0.2121 | 4 | 1  | 13    | 1842  | 1979   | 0.4190 | 5      | 1  | 9   | 9    | 1201   | 1087   | 0.7149 |        |
| 2 | 0 | 8    | 459  | 757    | 0.7049 | 4 | 1  | 14    | 982   | 708    | 0.2176 | 5      | 1  | 10  | 10   | 672    | 472    | 0.3234 |        |
| 3 | 1 | 9    | 2176 | 1923   | 0.4110 | 4 | 1  | 15    | 625   | 1011   | 0.3101 | 5      | 1  | 11  | 11   | 298    | 158    | 0.4244 |        |
| 2 | 0 | 10   | 2470 | 2041   | 0.3323 | 4 | 1  | 16    | 625   | 683    | 0.0443 | 5      | 1  | 12  | 13   | 883    | 758    | 0.8044 |        |
| 3 | 1 | 11   | 990  | 923    | 0.4487 | 4 | 1  | 17    | 1600  | 1295   | 0.5000 | 5      | 1  | 14  | 14   | 527    | 333    | 0.6950 |        |
| 2 | 0 | 12   | 1481 | 1421   | 0.8662 | 4 | 1  | 18    | 6584  | 8797   | 0.6117 | 5      | 1  | 15  | 15   | 360    | 155    | 0.4616 |        |
| 3 | 1 | 13   | 150  | 1405   | 0.1151 | 4 | 1  | 19    | 2510  | 2191   | 0.5970 | 5      | 1  | 16  | 16   | 324    | 250    | 0.5011 |        |
| 2 | 0 | 14   | 886  | 784    | 0.4331 | 4 | 1  | 20    | 443   | 442    | 0.5955 | 5      | 1  | 17  | 17   | 324    | 540    | 0.3968 |        |
| 3 | 1 | 15   | 677  | 699    | 0.9999 | 4 | 1  | 21    | 2494  | 2578   | 0.5857 | 5      | 1  | 18  | 18   | 3157   | 1766   | 0.5161 |        |
| 2 | 0 | 16   | 1599 | 1671   | 0.8774 | 4 | 1  | 22    | 10324 | 8088   | 0.8883 | 5      | 1  | 19  | 19   | 2245   | 2212   | 0.1273 |        |
| 3 | 1 | 17   | 2057 | 2040   | 0.5938 | 4 | 1  | 23    | 3549  | 3765   | 0.5732 | 5      | 1  | 20  | 20   | 985    | 861    | 0.3719 |        |
| 2 | 0 | 18   | 7651 | 8801   | 0.7485 | 4 | 1  | 24    | 2964  | 2823   | 0.7939 | 5      | 1  | 21  | 21   | 870    | 1455   | 0.9975 |        |
| 3 | 1 | 19   | 2346 | 2345   | 0.4114 | 4 | 1  | 25    | 1295  | 1347   | 0.6802 | 5      | 1  | 22  | 22   | 294    | 252    | 0.5883 |        |
| 2 | 0 | 20   | 800  | 800    | 0.3462 | 4 | 1  | 26    | 301   | 287    | 0.6463 | 5      | 1  | 23  | 23   | 521    | 600    | 0.5227 |        |
| 3 | 1 | 21   | 6296 | 1247   | 0.4923 | 4 | 1  | 27    | 1736  | 1671   | 0.6465 | 5      | 1  | 24  | 24   | 559    | 603    | 0.1986 |        |
| 2 | 0 | 22   | 6707 | 5945   | 0.9312 | 4 | 1  | 28    | 4777  | 4484   | 0.8156 | 5      | 1  | 25  | 25   | 511    | 612    | 0.0957 |        |
| 3 | 1 | 23   | 1177 | 1295   | 0.6777 | 4 | 1  | 29    | 906   | 868    | 0.6740 | 5      | 1  | 26  | 26   | 324    | 353    | 0.2277 |        |
| 2 | 0 | 24   | 929  | 1275   | 0.7754 | 4 | 1  | 30    | 1076  | 1123   | 0.2822 | 5      | 1  | 27  | 27   | 365    | 392    | 0.2146 |        |
| 3 | 1 | 25   | 956  | 928    | 0.8729 | 4 | 1  | 31    | 204   | 204    | 0.2652 | 5      | 1  | 28  | 28   | 267    | 169    | 0.5152 |        |
| 2 | 0 | 26   | 656  | 677    | 0.9999 | 4 | 1  | 32    | 2074  | 2293   | 0.1010 | 5      | 1  | 29  | 29   | 789    | 758    | 1.0000 |        |
| 3 | 1 | 27   | 1599 | 1671   | 0.8774 | 4 | 1  | 33    | 2148  | 2155   | 0.8344 | 5      | 1  | 30  | 30   | 793    | 654    | 0.1928 |        |
| 2 | 0 | 28   | 659  | 700    | 0.7913 | 4 | 1  | 34    | 5679  | 6551   | 0.0760 | 5      | 1  | 31  | 31   | 148    | 148    | 0.5797 |        |
| 3 | 1 | 29   | 733  | 733    | 0.6510 | 4 | 1  | 35    | 2925  | 3175   | 0.2766 | 5      | 1  | 32  | 32   | 124    | 1148   | 0.5442 |        |
| 2 | 0 | 30   | 247  | 219    | 0.2173 | 4 | 1  | 36    | 1007  | 1007   | 0.6414 | 5      | 1  | 33  | 33   | 1139   | 990    | 0.3254 |        |
| 3 | 1 | 31   | 3322 | 1441   | 1.0000 | 4 | 1  | 37    | 4138  | 4691   | 0.8904 | 5      | 1  | 34  | 34   | 352    | 105    | 0.2415 |        |
| 2 | 0 | 32   | 2566 | 2293   | 0.0744 | 4 | 1  | 38    | 3309  | 3530   | 0.2435 | 5      | 1  | 35  | 35   | 346    | 368    | 0.2026 |        |
| 3 | 1 | 33   | 1051 | 1113   | 0.8904 | 4 | 1  | 39    | 7     | 3189   | 3340   | 0.4432 | 5  | 1   | 36   | 36     | 353    | 364    | 0.1908 |
| 2 | 0 | 34   | 3024 | 2661   | 0.5825 | 4 | 1  | 40    | 3633  | 4496   | 0.6477 | 5      | 1  | 37  | 37   | 321    | 488    | 0.4141 |        |
| 3 | 1 | 35   | 656  | 569    | 0.5133 | 4 | 1  | 41    | 5209  | 2781   | 0.6228 | 5      | 1  | 38  | 38   | 801    | 803    | 0.8090 |        |
| 2 | 0 | 36   | 1742 | 1632   | 0.3159 | 4 | 1  | 42    | 9     | 530    | 743    | 0.1468 | 5  | 1   | 39   | 39     | 566    | 542    | 0.4218 |
| 3 | 1 | 37   | 5998 | 4261   | 0.0121 | 4 | 1  | 43    | 911   | 1007   | 0.6414 | 5      | 1  | 40  | 40   | 413    | 49     | 0.5004 |        |
| 2 | 0 | 38   | 1078 | 1388   | 0.8466 | 4 | 1  | 44    | 2985  | 2644   | 0.2154 | 5      | 1  | 41  | 41   | 196    | 966    | 0.7932 |        |
| 3 | 1 | 39   | 430  | 782    | 0.2515 | 4 | 1  | 45    | 1969  | 1763   | 0.1942 | 5      | 1  | 42  | 42   | 124    | 115    | 0.1535 |        |
| 2 | 0 | 40   | 1080 | 1080   | 0.5225 | 4 | 1  | 46    | 6570  | 6590   | 0.5100 | 5      | 1  | 43  | 43   | 594    | 519    | 0.0106 |        |
| 3 | 1 | 41   | 2798 | 2543   | 0.4045 | 4 | 1  | 47    | 3119  | 3397   | 0.2934 | 5      | 1  | 44  | 44   | 626    | 519    | 0.0803 |        |
| 2 | 0 | 42   | 572  | 844    | 0.1400 | 4 | 1  | 48    | 2     | 3282   | 3595   | 0.1114 | 5  | 1   | 45   | 45     | 665    | 655    | 0.3297 |
| 3 | 1 | 43   | 1412 | 1296   | 0.0351 | 4 | 1  | 49    | 3     | 2155   | 2348   | 0.2788 | 5  | 1   | 46   | 46     | 672    | 655    | 0.7937 |
| 2 | 0 | 44   | 923  | 846    | 0.8661 | 4 | 1  | 50    | 4     | 3494   | 4394   | 0.6628 | 5  | 1   | 47   | 47     | 355    | 246    | 0.5780 |
| 3 | 1 | 45   | 1417 | 1170   | 0.3732 | 4 | 1  | 51    | 5     | 3254   | 3254   | 0.3049 | 5  | 1   | 48   | 48     | 521    | 521    | 0.4141 |
| 2 | 0 | 46   | 1694 | 1737   | 1.0000 | 4 | 1  | 52    | 1007  | 1007   | 0.6700 | 5      | 1  | 49  | 49   | 616    | 604    | 0.8234 |        |
| 3 | 1 | 47   | 2339 | 2262   | 0.2539 | 4 | 1  | 53    | 2374  | 2126   | 0.4404 | 5      | 1  | 50  | 50   | 249    | 316    | 0.7905 |        |
| 2 | 0 | 48   | 3248 | 3222   | 0.2568 | 4 | 1  | 54    | 7     | 1194   | 1150   | 0.2693 | 5  | 1   | 51   | 51     | 804    | 722    | 0.1000 |
| 3 | 1 | 49   | 3194 | 3194   | 0.4489 | 4 | 1  | 55    | 4     | 4424   | 4522   | 0.7940 | 5  | 1   | 52   | 52     | 473    | 425    | 0.3295 |
| 2 | 0 | 50   | 1444 | 150    | 0.9300 | 4 | 1  | 56    | 2688  | 2431   | 0.9976 | 5      | 1  | 53  | 53   | 495    | 454    | 0.4559 |        |
| 3 | 1 | 51   | 2532 | 2998   | 0.7115 | 4 | 1  | 57    | 2626  | 2592   | 0.9972 | 5      | 1  | 54  | 54   | 504    | 489    | 0.4929 |        |
| 2 | 0 | 52   | 2891 | 2864   | 0.4462 | 4 | 1  | 58    | 7     | 2558   | 3080   | 0.8802 | 5  | 1   | 55   | 55     | 577    | 577    | 0.3954 |
| 3 | 1 | 53   | 1015 | 1202   | 0.0176 | 4 | 1  | 59    | 8     | 1392   | 1653   | 0.8729 | 5  | 1   | 56   | 56     | 433    | 276    | 0.6415 |
| 2 | 0 | 54   | 764  | 992    | 0.3250 | 4 | 1  | 60    | 9     | 1988   | 1891   | 0.7133 | 5  | 1   | 57   | 57     | 80     | 684    | 0.5000 |
| 3 | 1 | 55   | 257  | 2707   | 0.2173 | 4 | 1  | 61    | 10    | 1899   | 1768   | 0.5895 | 5  | 1   | 58   | 58     | 2      | 1975   | 2240   |
| 2 | 0 | 56   | 324  | 689    | 0.7331 | 4 | 1  | 62    | 5     | 2377   | 2353   | 0.3080 | 5  | 1   | 59   | 59     | 3      | 1946   | 1578   |
| 3 | 1 | 57   | 870  | 1187   | 0.8747 | 4 | 1  | 63    | 6     | 1677   | 1760   | 0.0126 | 5  | 1   | 60   | 60     | 4      | 3552   | 2656   |
| 2 | 0 | 58   | 1670 | 1670   | 0.8451 | 4 | 1  | 64    | 8     | 930    | 1057   | 0.1442 | 5  | 1   | 61   | 61     | 6      | 930    | 942    |
| 3 | 1 | 59   | 1226 | 1265   | 0.1221 | 4 | 1  | 65    | 10    | 1425   | 1427   | 0.1323 | 5  | 1   | 62   | 62     | 7      | 1249   | 1141   |
| 2 | 0 | 60   | 745  | 845    | 0.5130 | 4 | 1  | 66    | 11    | 1431   | 1381   | 0.2390 | 5  | 1   | 63   | 63     | 8      | 1057   | 1077   |
| 3 | 1 | 61   | 1634 | 1698   | 0.1135 | 4 | 1  | 67    | 7     | 777    | 816    | 1.0000 | 5  | 1   | 64   | 64     | 403    | 404    | 0.4242 |
| 2 | 0 | 62   | 170  | 150    | 0.9545 | 4 | 1  | 68    | 1     | 1658   | 1728   | 0.2723 | 5  | 1   | 65   | 65     | 451    | 451    | 0.8722 |
| 3 | 1 | 63   | 841  | 667    | 0.0459 | 4 | 1  | 69    | 2     | 2057   | 2013   | 0.5957 |    |     |      |        |        |        |        |

Table 3. Continued.

|   |   |     |      |       |        |   |   |     |      |        |        |    |   |    |      |       |        |
|---|---|-----|------|-------|--------|---|---|-----|------|--------|--------|----|---|----|------|-------|--------|
| 6 | 3 | 10  | 320  | 335   | 0.971  | 7 | 1 | 10  | 1111 | 1346   | 0.6462 | 7  | 6 | 4  | 1262 | 832   | 0.0467 |
| 6 | 4 | 11  | 746  | 786   | 0.970  | 7 | 1 | 11  | 1112 | 1404   | 0.3416 | 7  | 6 | 5  | 1246 | 949   | 0.8713 |
| 6 | 4 | 13  | 336  | 419   | 0.4378 | 7 | 1 | 12  | 1123 | 615    | 0.8373 | 7  | 6 | 5  | 1193 | 907   | 0.8756 |
| 6 | 4 | 1   | 1526 | 1593  | 1.0070 | 7 | 1 | 14  | 437  | 905    | 0.8375 | 7  | 6 | 5  | 1293 | 624   | 0.4718 |
| 6 | 4 | 1   | 535  | 446   | 0.9220 | 7 | 2 | 9   | 550  | 432    | 0.5001 | 7  | 6 | 8  | 1378 | 1134  | 0.1177 |
| 6 | 4 | 2   | 1289 | 1240  | 0.4491 | 7 | 2 | 1   | 1724 | 1324   | 0.8428 | 7  | 7 | 6  | 1048 | 992   | 0.3500 |
| 6 | 4 | 3   | 571  | 651   | 0.5158 | 7 | 2 | 2   | 1653 | 1510   | 0.5437 | 7  | 7 | 1  | 759  | 667   | 0.3419 |
| 6 | 4 | 791 | 955  | 0.970 | 7      | 2 | 0 | 375 | 372  | 0.7479 | 7      | 7  | 2 | 45 | 51   | 0.059 |        |
| 6 | 4 | 5   | 695  | 643   | 0.0161 | 7 | 2 | 4   | 1356 | 1245   | 0.8641 | 7  | 7 | 3  | 787  | 742   | 0.2473 |
| 6 | 4 | 6   | 405  | 637   | 0.4455 | 7 | 2 | 5   | 491  | 346    | 0.479  | 7  | 7 | 4  | 458  | 532   | 0.6499 |
| 6 | 4 | 8   | 565  | 718   | 0.8476 | 7 | 2 | 6   | 726  | 854    | 0.5251 | 8  | 0 | 2  | 1130 | 1228  | 0.6979 |
| 6 | 4 | 9   | 706  | 718   | 0.9476 | 7 | 2 | 7   | 3409 | 3470   | 0.9986 | 8  | 0 | 4  | 3570 | 2991  | 0.0463 |
| 6 | 4 | 10  | 291  | 345   | 0.4379 | 7 | 2 | 8   | 655  | 947    | 0.6410 | 8  | 0 | 6  | 1748 | 1011  | 0.1444 |
| 6 | 4 | 11  | 273  | 349   | 0.4336 | 7 | 2 | 9   | 1565 | 1650   | 0.502  | 8  | 0 | 8  | 748  | 601   | 0.2488 |
| 6 | 5 | 0   | 1191 | 966   | 0.5000 | 7 | 2 | 10  | 342  | 542    | 0.7115 | 8  | 0 | 10 | 2469 | 2973  | 0.1453 |
| 6 | 5 | 1   | 522  | 564   | 0.0480 | 7 | 2 | 11  | 586  | 819    | 0.0458 | 8  | 0 | 12 | 1421 | 1072  | 0.9456 |
| 6 | 5 | 2   | 1365 | 1234  | 0.9913 | 7 | 2 | 12  | 302  | 579    | 0.7188 | 8  | 1 | 0  | 527  | 661   | 0.5070 |
| 6 | 5 | 3   | 1257 | 1151  | 0.9743 | 7 | 2 | 13  | 1057 | 1243   | 0.8692 | 8  | 1 | 1  | 1334 | 1334  | 0.0375 |
| 6 | 5 | 5   | 233  | 329   | 0.8926 | 7 | 3 | 0   | 542  | 945    | 0.0490 | 8  | 1 | 2  | 1544 | 1717  | 0.4447 |
| 6 | 5 | 6   | 1235 | 1175  | 0.9726 | 7 | 3 | 1   | 1642 | 1380   | 0.4424 | 8  | 1 | 3  | 3106 | 3297  | 0.2492 |
| 6 | 5 | 7   | 446  | 534   | 0.5443 | 7 | 3 | 2   | 1080 | 876    | 0.8664 | 8  | 1 | 4  | 1570 | 1653  | 0.4433 |
| 6 | 5 | 8   | 881  | 864   | 0.3497 | 7 | 3 | 3   | 1102 | 1072   | 0.8048 | 8  | 1 | 5  | 1090 | 976   | 0.0412 |
| 6 | 5 | 9   | 255  | 327   | 0.9747 | 7 | 3 | 4   | 2864 | 3156   | 0.1477 | 8  | 1 | 6  | 2114 | 1984  | 0.0770 |
| 6 | 5 | 10  | 315  | 461   | 0.9483 | 7 | 3 | 5   | 525  | 746    | 0.2992 | 8  | 1 | 7  | 3124 | 3033  | 0.4472 |
| 6 | 5 | 12  | 324  | 447   | 0.4339 | 7 | 3 | 6   | 2157 | 2542   | 0.2932 | 8  | 1 | 8  | 2479 | 2332  | 0.5277 |
| 6 | 6 | 0   | 645  | 527   | 1.0000 | 7 | 3 | 7   | 655  | 718    | 0.9558 | 8  | 1 | 9  | 1631 | 1216  | 0.1994 |
| 6 | 6 | 1   | 938  | 1058  | 0.5162 | 7 | 3 | 10  | 1643 | 1743   | 0.1797 | 8  | 1 | 10 | 1378 | 274   | 0.4526 |
| 6 | 6 | 2   | 505  | 452   | 0.9745 | 7 | 3 | 12  | 706  | 857    | 0.0456 | 8  | 1 | 11 | 1165 | 1256  | 0.5662 |
| 6 | 6 | 3   | 387  | 276   | 0.0473 | 7 | 3 | 13  | 329  | 541    | 0.8017 | 8  | 0 | 0  | 73   | 65    | 0.0101 |
| 6 | 6 | 4   | 746  | 622   | 0.4787 | 7 | 4 | 0   | 829  | 666    | 1.0000 | 8  | 1 | 1  | 3156 | 3250  | 0.6174 |
| 6 | 6 | 5   | 355  | 313   | 0.5912 | 7 | 4 | 1   | 1996 | 1437   | 0.3190 | 8  | 2 | 2  | 631  | 964   | 0.5868 |
| 6 | 6 | 7   | 581  | 639   | 0.9499 | 7 | 4 | 2   | 2982 | 2179   | 0.6559 | 8  | 2 | 3  | 1464 | 1799  | 0.9923 |
| 6 | 6 | 9   | 173  | 384   | 0.3182 | 7 | 4 | 3   | 2836 | 1838   | 0.2733 | 8  | 2 | 4  | 4553 | 959   | 0.5910 |
| 6 | 7 | 0   | 277  | 67    | 0.9998 | 7 | 4 | 4   | 2254 | 1822   | 0.3597 | 8  | 2 | 5  | 2459 | 2491  | 0.4460 |
| 6 | 7 | 1   | 478  | 389   | 0.9465 | 7 | 4 | 5   | 921  | 921    | 0.2992 | 8  | 2 | 6  | 1742 | 1472  | 0.5277 |
| 6 | 7 | 2   | 272  | 288   | 0.3491 | 7 | 4 | 7   | 639  | 736    | 0.3723 | 8  | 2 | 7  | 1164 | 1168  | 0.7455 |
| 6 | 7 | 3   | 325  | 298   | 0.5452 | 7 | 4 | 8   | 1066 | 1171   | 0.5334 | 8  | 3 | 0  | 703  | 991   | 1.0000 |
| 6 | 7 | 5   | 291  | 449   | 0.8485 | 7 | 4 | 9   | 748  | 974    | 0.3453 | 8  | 3 | 2  | 2146 | 2046  | 0.4721 |
| 6 | 7 | 7   | 302  | 677   | 0.3902 | 7 | 4 | 10  | 431  | 431    | 0.1332 | 8  | 3 | 3  | 592  | 1304  | 0.3350 |
| 6 | 8 | 1   | 278  | 520   | 0.5304 | 7 | 4 | 11  | 243  | 564    | 0.8585 | 8  | 3 | 4  | 2456 | 2597  | 0.9359 |
| 6 | 8 | 2   | 263  | 412   | 0.9165 | 7 | 4 | 12  | 655  | 1063   | 0.2771 | 8  | 3 | 5  | 1907 | 1850  | 0.8511 |
| 6 | 8 | 3   | 231  | 387   | 0.9249 | 7 | 5 | 1   | 2199 | 1766   | 0.6877 | 8  | 3 | 6  | 1977 | 1511  | 0.2776 |
| 6 | 8 | 2   | 452  | 459   | 0.9700 | 7 | 5 | 2   | 2193 | 1866   | 0.5100 | 8  | 3 | 8  | 1872 | 1933  | 0.3222 |
| 7 | 0 | 2   | 2127 | 2046  | 0.9398 | 7 | 5 | 3   | 645  | 636    | 0.0193 | 8  | 4 | 0  | 278  | 2733  | 0.5100 |
| 7 | 0 | 6   | 1564 | 1796  | 0.2401 | 7 | 5 | 4   | 2649 | 1767   | 0.0195 | 8  | 4 | 1  | 1673 | 1586  | 0.2824 |
| 7 | 0 | 8   | 3266 | 3520  | 0.0732 | 7 | 5 | 5   | 608  | 556    | 0.7146 | 8  | 4 | 2  | 1674 | 1473  | 0.1414 |
| 7 | 0 | 12  | 1383 | 1736  | 0.2920 | 7 | 5 | 7   | 669  | 745    | 0.6423 | 8  | 4 | 3  | 1183 | 1223  | 0.2715 |
| 7 | 0 | 14  | 697  | 1049  | 0.2466 | 7 | 5 | 8   | 540  | 724    | 0.6866 | 8  | 4 | 5  | 197  | 1631  | 0.3351 |
| 7 | 1 | 0   | 2835 | 3429  | 0.5040 | 7 | 5 | 9   | 404  | 1041   | 0.9846 | 8  | 5 | 1  | 503  | 1177  | 0.4141 |
| 7 | 1 | 1   | 2937 | 3497  | 0.1719 | 7 | 5 | 10  | 456  | 9746   | 0.7465 | 8  | 5 | 2  | 505  | 771   | 0.3851 |
| 7 | 1 | 2   | 879  | 930   | 0.2933 | 7 | 6 | 0   | 491  | 437    | 1.0000 | 8  | 5 | 3  | 2384 | 1904  | 0.7934 |
| 7 | 1 | 3   | 924  | 1016  | 0.4142 | 7 | 6 | 1   | 1095 | 966    | 0.5431 | 8  | 5 | 6  | 879  | 1250  | 0.4497 |
| 7 | 1 | 4   | 1993 | 2010  | 0.0707 | 7 | 6 | 2   | 1569 | 1118   | 0.0479 | 8  | 6 | 0  | 6672 | 3580  | 1.0000 |
| 7 | 1 | 5   | 2916 | 2548  | 0.3116 | 7 | 6 | 3   | 671  | 685    | 0.2233 | 8  | 6 | 0  | 7341 | 7274  | 1.0000 |
| 7 | 1 | 6   | 944  | 1129  | 0.4015 | 7 | 1 | 9   | 1560 | 2063   | 0.4992 | 10 | 0 | 0  | 609  | 266   | 0.5000 |

sible to decide which possibility is the correct one. The principal aim of this investigation was to establish the coordination about the chromium atoms, which is unaffected by either alternative. Since all other atoms fit the orthorhombic space group and since the structure of the ethylenediamine molecule is wellknown, the authors have chosen to describe the structure in terms of the space group  $Pmc_2_1$  with the carbon atoms statistically occupying two four-fold positions.

*Structure refinement.* At this stage of the structure determination the  $R$ -value was 0.20. The structure was then refined by the structure factor least-squares method using all 866 observed reflexions. For each reflexion the weight  $w$  was computed according to  $w=[1+(|F_o|-a)b^2]^{-1}$  with  $a=50$  and  $b=40$ . Anisotropic temperature factors were used for all heavy atoms and isotropic ones for the light atoms. After about ten cycles the refinement converged to the parameters given in Table 2, the final  $R$ -value being 0.117.

Observed and calculated structure factors are given in Table 3. Calculated bond distances and angles and their standard deviations are given in Table 4 and some packing distances in Table 5. All bond distances were found to be within the normal range, thus supporting the correctness of the structure.

The result obtained from the refinement was further checked by calculating a three-dimensional electron density difference map. This showed only small residual maxima or minima, the largest maximum having a magnitude of about 15 % of the height of a true nitrogen peak in the  $|F_o|$ -synthesis.

Table 4. Bond distances and angles in the *trans*-dichloridodiaquaethylenediaminechromium(III) ion.

|                                       | Distance<br>(Å) | e.s.d.<br>(Å) |                                       | Distance<br>(Å) | e.s.d.<br>(Å) |
|---------------------------------------|-----------------|---------------|---------------------------------------|-----------------|---------------|
|                                       | Angle<br>(°)    | e.s.d.<br>(°) |                                       | Angle<br>(°)    | e.s.d.<br>(°) |
| $\text{Cr}_1-\text{Cl}_1$             | 2.32            | 0.01          | $\text{Cr}_2-\text{Cl}_2$             | 2.32            | 0.00          |
| $\text{Cr}_1-\text{O}_1$              | 2.02            | 0.02          | $\text{Cr}_2-\text{O}_3$              | 2.09            | 0.02          |
| $\text{Cr}_1-\text{O}_2$              | 2.04            | 0.02          | $\text{Cr}_2-\text{O}_4$              | 2.03            | 0.02          |
| $\text{Cr}_1-\text{N}_1$              | 2.08            | 0.02          | $\text{Cr}_2-\text{N}_3$              | 2.08            | 0.03          |
| $\text{Cr}_1-\text{N}_2$              | 2.12            | 0.02          | $\text{Cr}_2-\text{N}_4$              | 2.04            | 0.02          |
| $\text{N}_1-\text{C}_1$               | 1.41            | 0.05          | $\text{N}_3-\text{C}_3$               | 1.48            | 0.07          |
| $\text{N}_1-\text{C}_2$               | 1.60            | 0.07          | $\text{N}_4-\text{C}_4$               | 1.48            | 0.04          |
| $\text{C}_1-\text{C}_2$               | 1.58            | 0.06          | $\text{C}_3-\text{C}_4$               | 1.71            | 0.07          |
| $\text{Cl}_1-\text{Cr}_1-\text{Cl}_1$ | 179.3           | 0.3           | $\text{Cl}_2-\text{Cr}_2-\text{Cl}_2$ | 178.9           | 0.3           |
| $\text{Cl}_1-\text{Cr}_1-\text{O}_1$  | 90.0            | 0.2           | $\text{Cl}_2-\text{Cr}_2-\text{O}_3$  | 90.1            | 0.2           |
| $\text{Cl}_1-\text{Cr}_1-\text{O}_2$  | 89.7            | 0.2           | $\text{Cl}_2-\text{Cr}_2-\text{O}_4$  | 90.5            | 0.2           |
| $\text{Cl}_1-\text{Cr}_1-\text{N}_1$  | 90.0            | 0.2           | $\text{Cl}_2-\text{Cr}_2-\text{N}_3$  | 89.4            | 0.2           |
| $\text{Cl}_1-\text{Cr}_1-\text{N}_2$  | 90.3            | 0.2           | $\text{Cl}_2-\text{Cr}_2-\text{N}_4$  | 89.8            | 0.2           |
| $\text{O}_1-\text{Cr}_1-\text{O}_2$   | 97.3            | 0.9           | $\text{O}_2-\text{Cr}_2-\text{O}_4$   | 96.1            | 0.8           |
| $\text{O}_1-\text{Cr}_1-\text{N}_1$   | 172.2           | 0.9           | $\text{O}_3-\text{Cr}_2-\text{N}_4$   | 171.1           | 0.9           |
| $\text{O}_1-\text{Cr}_1-\text{N}_2$   | 90.1            | 0.9           | $\text{O}_3-\text{Cr}_2-\text{N}_3$   | 87.1            | 0.9           |
| $\text{O}_2-\text{Cr}_1-\text{N}_1$   | 90.5            | 0.9           | $\text{O}_4-\text{Cr}_2-\text{N}_4$   | 92.8            | 0.9           |
| $\text{O}_2-\text{Cr}_1-\text{N}_2$   | 172.6           | 1.0           | $\text{O}_4-\text{Cr}_2-\text{N}_3$   | 176.9           | 0.9           |
| $\text{N}_1-\text{Cr}_1-\text{N}_2$   | 82.1            | 1.0           | $\text{N}_4-\text{Cr}_2-\text{N}_3$   | 84.0            | 1.0           |
| $\text{Cr}_1-\text{N}_1-\text{C}_1$   | 112.0           | 2.2           | $\text{Cr}_2-\text{N}_3-\text{C}_3$   | 115.1           | 2.8           |
| $\text{Cr}_1-\text{N}_2-\text{C}_2$   | 109.0           | 2.1           | $\text{Cr}_2-\text{N}_4-\text{C}_4$   | 112.7           | 2.0           |
| $\text{N}_1-\text{C}_1-\text{C}_2$    | 110.4           | 3.7           | $\text{N}_3-\text{C}_3-\text{C}_4$    | 104.1           | 3.8           |
| $\text{N}_2-\text{C}_2-\text{C}_1$    | 103.4           | 3.7           | $\text{N}_4-\text{C}_4-\text{C}_3$    | 109.9           | 3.0           |

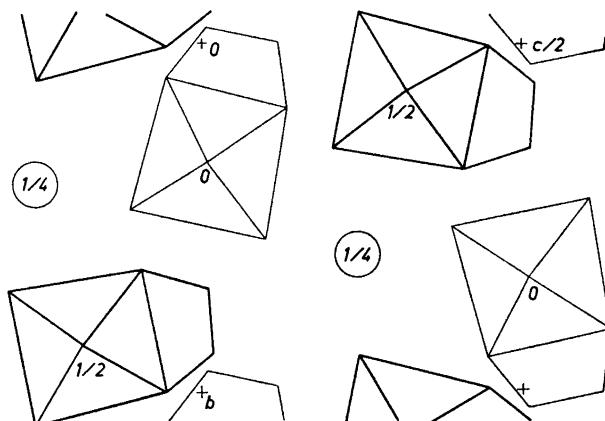


Fig. 1. The packing of the ions in *trans*- $[\text{CrCl}_2(\text{H}_2\text{O})_8\text{en}]\text{Cl}$  as viewed along the  $x$ -direction.

Table 5. Packing distances in *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl. (The first atom symbols refer to the coordinates given in Table 2. After the second atom symbols stand, within brackets, the unit cell translations in the *a*, *b*, and *c* directions and after that the number of the symmetry operation performed on the original coordinates of the atom as given in the International Tables for X-ray Crystallography Vol. I).

|                                  |           |        |
|----------------------------------|-----------|--------|
| Cl <sub>1</sub> —Cl <sub>1</sub> | (0 0 0)2  | 4.18 Å |
| —Cl <sub>2</sub>                 | (0 -1 0)1 | 4.47   |
| —Cl <sub>2</sub>                 | (0 0 0)1  | 4.56   |
| —Cl <sub>3</sub>                 | (0 0 0)1  | 3.78   |
| —Cl <sub>3</sub>                 | (0 -1 0)1 | 4.08   |
| —N <sub>3</sub>                  | (0 0 0)1  | 3.35   |
| —N <sub>4</sub>                  | (0 -1 0)1 | 3.25   |
| —C <sub>3</sub>                  | (0 -1 0)1 | 3.46   |
| —C <sub>4</sub>                  | (0 1 0)4  | 3.36   |
| Cl <sub>2</sub> —Cl <sub>2</sub> | (1 0 0)2  | 4.16   |
| —Cl <sub>3</sub>                 | (0 0 0)1  | 3.95   |
| —Cl <sub>3</sub>                 | (0 1 0)4  | 3.84   |
| —O <sub>1</sub>                  | (1 1 0)3  | 3.41   |
| —N <sub>1</sub>                  | (0 1 0)1  | 3.39   |
| —N <sub>2</sub>                  | (0 0 0)1  | 3.51   |
| —C <sub>2</sub>                  | (1 0 0)2  | 3.29   |
| Cl <sub>3</sub> —O <sub>1</sub>  | (0 0 0)1  | 3.28   |
| —O <sub>2</sub>                  | (0 0 0)1  | 3.05   |
| —O <sub>3</sub>                  | (0 0 0)1  | 3.02   |
| —O <sub>4</sub>                  | (0 0 0)1  | 3.17   |
| —C <sub>2</sub>                  | (1 1 -1)3 | 3.80   |
| —C <sub>3</sub>                  | (0 0 0)1  | 3.84   |
| O <sub>3</sub> —C <sub>3</sub>   | (0 0 0)1  | 3.31   |
| —C <sub>4</sub>                  | (0 0 0)1  | 3.20   |

#### DESCRIPTION AND DISCUSSION OF THE STRUCTURE

The crystals of Weinmann's blue, [CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]Cl, consist of dichlorido-diaquoethylenediamine ions and chloride ions as illustrated in Fig. 1. The complex ion is shown in Fig. 2. The structure investigation has shown that

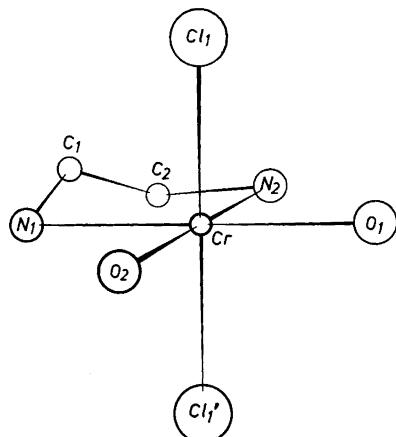


Fig. 2. The complex ion *trans*-[CrCl<sub>2</sub>(H<sub>2</sub>O)<sub>2</sub>en]<sup>+</sup>.

the two chlorine atoms of the octahedral complex are situated in *trans* positions. The two water molecules and the two nitrogen atoms of the ethylenediamine molecule are situated at the corners of a somewhat distorted square. These atoms together with the chromium atom lie in a crystallographic mirror plane.

In the course of the structure determination it became obvious that there are two possible solutions, one being based on space group  $Pc$  and the other on space group  $Pmc2_1$ . They cannot be distinguished experimentally. Following the arguments given above, the authors have chosen to describe the structure in terms of space group  $Pmc2_1$  instead of  $Pc$ . This means that the two carbon atoms of the ethylenediamine molecule statistically occupy four-fold positions (half-filled) in such a way that  $C_1$  and  $C_2$  are situated on opposite sides of the mirror planes one way or the other throughout the crystal. The same statistical manner was also chosen by Stomberg<sup>12</sup> in describing  $[\text{Cr}(\text{O}_2)_2(\text{H}_2\text{O})\text{en}](\text{H}_2\text{O})$ .

The Cr—Cl bond lengths are all 2.32 Å which compares well with the value 2.33 Å found by Ooi *et al.*<sup>13</sup> in  $[\text{CrCl}_2\text{en}_2]\text{Cl}\cdot\text{HCl}\cdot 2\text{H}_2\text{O}$ . The distances between the chromium and oxygen atoms lie between 2.02 and 2.09 Å, which is normal for a Cr—O<sub>water</sub> bond; 2.03 Å was found in  $[\text{Cr}(\text{O}_2)_2(\text{H}_2\text{O})\text{en}](\text{H}_2\text{O})$ .<sup>12</sup> The Cr—N bond distances are 2.04—2.12 Å and thus not significantly different, the mean value being 2.08 Å. 2.06 Å was found in  $[\text{Cr}(\text{O}_2)_2(\text{H}_2\text{O})\text{en}](\text{H}_2\text{O})$ ,<sup>12</sup> 2.12 Å in both  $[\text{CrCl}_2\text{en}_2]\text{Cl}\cdot\text{HCl}\cdot 2\text{H}_2\text{O}$ <sup>13</sup> and  $[\text{Cr}(\text{O}_2)_2(\text{NH}_3)_3]$ <sup>14</sup> (see also Ref. 15).

The errors in the positional parameters of the carbon atoms are, as expected, rather large, the standard deviations being about 0.07 Å as compared with 0.02 for nitrogen. The C—C and C—N bond lengths are, therefore, quite uncertain as well as the angles N—C—C and Cr—N—C but they do not differ significantly from their normal values.

The two independent N—Cr—N angles are not significantly different, being 82.1° and 84.0°. The value 82.6° was obtained for  $[\text{Cr}(\text{O}_2)_2(\text{H}_2\text{O})\text{en}](\text{H}_2\text{O})$ <sup>12</sup> and 85.2° for  $[\text{CrCl}_2\text{en}_2]\text{Cl}\cdot\text{HCl}\cdot 2\text{H}_2\text{O}$ .<sup>13</sup>

*Acknowledgements.* We wish to thank Professors C. Brosset and G. Lundgren for their continuous support. Part of the work has been sponsored by the *Swedish Natural Science Research Council* whose grant we greatly acknowledge. Finally we wish to thank Professor S. Abrahamsson for putting the programmes for the SAAB D21 computer at our disposal.

## REFERENCES

- House, D. A. and Garner, C. S. *Inorg. Chem.* **5** (1966) 840.
- Weinmann, E. *Thesis*, Zürich 1919.
- Weinmann, E. In Pascal, P. *Nouveau Traité de Chimie Minérale 14*, Masson Co., Paris 1959, p. 479.
- House, D. A. *Private communication*.
- Hambling, P. *Acta Cryst.* **6** (1953) 98.
- Abrahamsson, S. and Larsson, K. *Arkiv Kemi* **24** (1965) 383.
- Abrahamsson, S. *Arkiv Kemi* **24** (1965) 389.
- Aleby, S. *Arkiv Kemi* **24** (1965) 395.
- Larsson, K. *Arkiv Kemi* **23** (1964) 17.

10. Abrahamsson, S., Nilsson, B. and Selin, K. *Arkiv Kemi* **24** (1965) 407.
11. Lindqvist, O. and Wengelin, F. *Arkiv Kemi* **28** (1967) 179.
12. Stomberg, R. *Arkiv Kemi* **24** (1965) 47.
13. Ooi, S., Komiyama, Y. and Kuroya, H. *Bull. Chem. Soc. Japan* **33** (1960) 354.
14. Stomberg, R. *Arkiv Kemi* **22** (1964) 49.
15. *Tables of interatomic distances and configuration in molecules and ions*, The Chemical Society, London 1958.

Received June 20, 1968.